

On  
non-geometric  
string vacua

A few words  
on string  
theory

T-duality and  
non-geometry

Flux Com-  
pactifications

Flux Compact-  
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# On non-geometric string vacua

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## preliminary declaration...

We are working in string theory on

**generalised flux compactifications,**

at the convergence of two active fields of research: **Generalized  
Geometry** and **Flux Compactifications**.

*Let me explain what it is (as simply as I can)...*

# Outline

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# A few words on string theory

## definition and features

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a candidate theory of quantum gravity and other fields ultimately aiming to mimic our physical world (de Sitter, inflationary vacuum, Standard Model etc...)

- 1 Supersymmetric (SUSY) theory with a length scale  $l_s \sim \sqrt{\alpha'}$ , perturbatively formulated only in ten dimensions

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- 2 5 versions: Type IIA, Type IIB, Type I, Heterotic  $SO(32)/E_8 \times E_8$

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- 1 Supersymmetric (SUSY) theory with a length scale  $l_s \sim \sqrt{\alpha'}$ , perturbatively formulated only in ten dimensions
- 2 5 versions: Type IIA, Type IIB, Type I, Heterotic  $SO(32)/E_8 \times E_8$
- 3 Every theory has a (universal) bosonic supergravity (SUGRA) sector: graviton  $g_{\mu\nu}$ , 2-form gauge field  $B_{\mu\nu}$ , scalar (dilaton)  $\phi$

# T-duality and non-geometry

## T-duality on a circle

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T-duality is a perturbative symmetry between two string theories with compactified dimensions

How it works for string theories compactified on circles:

- 1 Consider a string theory compactified on a circle  $S^1$  of radius  $R$  and coordinate  $X$  ( $D=10 \rightarrow D=9$  dimensions)

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- 3 The string winds around the circle in units of  $2\pi R$ :  
 $\Delta X = 2\pi Rm$  ( $m \in \mathbb{Z}$ )

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- 4 **T-duality:**  $R \rightarrow \alpha'/R$  and  $n \leftrightarrow m$

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**T-duality:**  $R \rightarrow \alpha'/R$  and  $n \leftrightarrow m$



- 1 Crucial: T-duality means that string theories with  $R \geq \sqrt{\alpha'}$  and  $R \leq \sqrt{\alpha'}$  are identified
- 2 In other words, the string cannot distinguish between big radii and small radii!

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## T-duality on a torus

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Generalization: How T-duality works for string theories compactified on a torus  $T^d$  (product of  $d$  circles)



- 1 Along the directions  $(a, b)$  of  $T^d$ , the fields are:  $g_{ab}, B_{ab}$  and  $\phi = \phi_0$  (frozen out)

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- 2 The fields can be embedded in a  $2d \times 2d$  matrix

$$\mathcal{H} = \begin{bmatrix} g^{-1} & -g^{-1}B \\ Bg^{-1} & g - bg^{-1}b \end{bmatrix}$$

# T-duality and non-geometry

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- 3 **T-duality**:  $\mathcal{H} \rightarrow O\mathcal{H}O^T$ ,  $O \in O(d, d; \mathbb{Z})$
- 4 Crucial: T-duality mixes the metric  $g$  with the gauge field  $B$  in a non trivial way: **the string treats on the same footing the fields  $g$  and  $B$ !**

# T-duality and non-geometry

non-geometry...

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So... 2 significant slogans by T-duality:

- 1 The string cannot distinguish between big radii and small radii
- 2 The string treats on the same footing the fields  $g$  and  $B$ , mixing them in a non-trivial way



important hints that classical notion of Riemannian geometry breaks down at  $l_s \sim \sqrt{\alpha'}$ , to be replaced by a stringy geometry.

- 1 Clarification → **Non-Geometric  $\equiv$  Non-Riemannian**



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important hints that classical notion of Riemannian geometry breaks down at  $l_s \sim \sqrt{\alpha'}$ , to be replaced by a stringy geometry.

- 1 Clarification  $\rightarrow$  **Non-Geometric  $\equiv$  Non-Riemannian**
- 2 Non-geometric string backgrounds can be constructed: at the overlap of coordinate charts the transition functions are other than diffeomorphisms and gauge field transformations of  $B_{\mu\nu}$

# T-duality and non-geometry

example of a non-geometric background: T-fold

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Consider the NS5-brane background, i.e. the  $D = 10$  background due to an extended five-dimensional object of string theory called NS5-brane

The NS5-brane has 4 spatial directions orthogonal to it:  
 $x^1, x^2, x^3, x^4$

Compactifying  $x^1$  and  $x^2$  on circles and performing two T-dualities [De Boer, Shigemori]:

NS5-brane  $\xrightarrow{x^1, x^2}$  T-fold

# T-duality and non-geometry

example of a non-geometric background: T-fold

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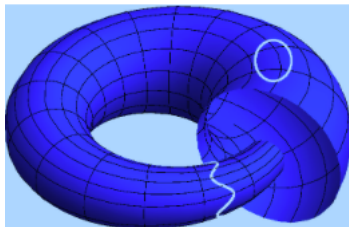
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Compactifying  $x^1$  and  $x^2$  on circles and performing two T-dualities [De Boer, Shigemori]:

$$\text{NS5-brane} \xrightarrow{x^1, x^2} \text{T-fold}$$

The T-fold is non-geometric:

The fields  $g$  and  $B$  match via non-geometric transition functions



# T-duality and non-geometry

another view on the T-duality chain

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Pointing out that the NS5-brane is charged under the gauge field  $B_{\mu\nu}$ , with field strength  $H_3 = dB_2...$

NS5-brane  $\xrightarrow{x^1, x^2}$  T-fold

can be thought of as a chain of fluxes:

$H_3 \xrightarrow{x^1} f_3 \xrightarrow{x^2} Q_3$

1 **fluxes** : field strengths of gauge form fields

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- 1 **fluxes** : field strengths of gauge form fields
- 2  **$Q_3$** : most simple example of non-geometric flux

# Flux Compactifications

making contact with the physics of our world...

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## Steps towards construction of realistic 4D string models :

- 1 In order to go from  $D=10 \rightarrow D=4$  ... compactify on 6-dimensional manifolds with a non-trivial topology to break SUSY: Calabi-Yau (CY) 3-folds and/or singular limits of them (orbifolds)

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Steps towards construction of realistic 4D string models :

- 1 In order to go from  $D=10 \rightarrow D=4$  ... compactify on 6-dimensional manifolds with a non-trivial topology to break SUSY: Calabi-Yau (CY) 3-folds and/or singular limits of them (orbifolds)
- 2 Turn on 3-form fluxes with legs on CY in order to generate a four-dimensional potential and give mass to the moduli fields (**moduli stabilisation**). Moduli fields are 4D massless scalar fields parameterising the geometry of CY and need mass to agree with experiments. Famous moduli stabilisation scenarios are: KKLT, LVS. Also, they try to mimic the microphysics of inflation [Kachru et al.], [Quevedo F. et al]

# Flux Compactifications and non-geometry why?

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What about the possibility to compactify turning on non-geometric fluxes (ngf)?

Motivations:

- 1 **T-duality “cries out” for ngf**: if you want a 4D model with *generic* geometric fluxes, consistency with T-duality requires ngf
- 2 Non-geometric (Generalized) flux compactifications allow to stabilise all the moduli at tree-level (in the standard case you have to consider perturbative, non-perturbative corrections)
- 3 Richness for phenomenology (waiting to be discovered)



# Flux Compactifications and non-geometry

what we know

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One more look at the previous fluxes chain :

$$H_3 \xrightarrow{T} f_3 \xrightarrow{T} Q_3 \xrightarrow{T} R_3$$

- 1 One can extend this chain considering S-dual of these fluxes: **P-fluxes**. In a recent paper we have classified P-fluxes in supergravity. [E.A. Bergshoeff , V.A. Penas , F. Riccioni and S.R.]
- 2 There have been built explicit type IIA/B string models which use the fluxes  $Q, R$  [Shelton *et al.*][Aldazabal *et al.*]
- 3 There is some model of generalised moduli stabilisation reproducing the microphysics of inflation [Blumenhagen *et al.*][Lust *et al.*][Damian C. *et al.*]

# Flux Compactifications and non-geometry

perspectives: what we want to know

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We are currently looking for...

- 1 ... finding and studying consistent models of compactification taking into account for all P-fluxes
- 2 ... describing new generalized flux vacua in terms of equivalent conformal field theories related to compactifications on *special* orbifolds.
- 3 ... monitoring the models of inflation and trying to understand the role of non-geometric fluxes